

Consider an ideal simple harmonic oscillator (A mass on a spring). The mass of the block is 2kg. A force of 20N stretches the spring to a displacement of .5m.

1. What is the spring constant?

40 N/m

$$F = Kx$$

$$K = \frac{20}{.5} = 40 \text{ N/m}$$

2. What is the total energy of the oscillator?

5 J

$$U = \frac{1}{2} K x^2 = \frac{1}{2} (40) (.5)^2 = 5 \text{ J}$$

3. What is the velocity of the mass at .3m?

1.79 m/s

$$U = \frac{1}{2} 40 (.3)^2 = 1.8$$

$$5 - 1.8 = 3.2$$

$$3.2 = \frac{1}{2} m v^2$$

$$3.2 = \frac{1}{2} (2) v^2$$

4. What is its velocity at .4m?

1.34

$$U = \frac{1}{2} 40 (.4)^2 = 3.2$$

$$5 - 3.2 = 1.8$$

$$1.8 = \frac{1}{2} (2) v^2 = 1.34$$

5. What is its acceleration at $x = .5 \text{ m}$ and $x = -.5 \text{ m}$

-10 m/s² .5m

10 m/s² -.5m

$$ma = Kx$$

$$2a = 40(.5)$$

$$a = 10$$

6. What is its acceleration at .3m?

-6 m/s²

$$ma = Kx \quad 2a = 40(.3)$$

$$a = 6 \text{ m/s}^2$$

7. What is the net force on the mass at equilibrium?

0 N

8. What is the size of the net force at .25m?

-10 N

$$F = Kx \quad 40(.25) = 10 \text{ N}$$

9. The position of the oscillator where the Kinetic energy equals the Potential energy?

.353 m

5 J is total energy

$\frac{1}{2}$ is 2.5 J of each

$$2.5 = U$$

$$2.5 = \frac{1}{2} K x^2$$

$$2.5 = \frac{1}{2} (40) x^2$$

$$.353 \text{ m}$$

IN THESE PROBLEMS, THE MOTION IS ALWAYS HORIZONTAL...NEVER VERTICAL!

1. A 12cm spring has a force constant of 400N/m. How much force is required to stretch the spring to 14cm?

8 N

$$F = kx$$

$$F = 400 \cdot .02 = 8 \text{ N}$$

2. A 1.5kg block oscillates on a spring whose k value is 500N/m. The amplitude of the oscillations is 4cm. What is the maximum speed of the block?

.73 m/s

$$U_o = KE$$

$$\frac{1}{2} 500 (.04)^2 = \frac{1}{2} 1.5 v^2$$

$$\frac{1}{2} kx^2 = \frac{1}{2} mv^2$$

$$v = .73 \text{ m/s}$$

3. A 2 kg mass is attached to a spring with a k value of 500N/m. The amplitude of the oscillation is 8cm. Find

1.6 J

total energy present

$$U = \frac{1}{2} kx^2 = \frac{1}{2} 500 (.08)^2$$

$$U = \frac{1}{2} kx^2 = \frac{1}{2} 500 (.04)^2 = .4 \text{ J Elastic PE}$$

$$\begin{array}{r} 1.6 \text{ Total} \\ - .4 \text{ PE} \\ \hline 1.2 \text{ KE} \end{array}$$

1.09 m/s

The speed when it is 4cm from the resting point

$$1.2 = \frac{1}{2} (2) v^2 = 1.09$$

4. A 2kg block is attached to a spring (k=500N/m). The block rests at its equilibrium position. A force acts on the block to give it an initial speed of 2m/s. What is the amplitude of the oscillation?

$$KE = U$$

$$\frac{1}{2} 2 \cdot 2^2 = \frac{1}{2} 500 x^2$$

$$\frac{1}{2} mv^2 = \frac{1}{2} kx^2$$

.126 m

5. A block oscillating on a spring move from maximum stretch to compression in .25s. Find the period and frequency.

$$.25 \text{ s} = \frac{1}{2} \text{ a cycle} \quad .5 = 1 \text{ cycle}$$

.5 s

period

1/.5 = 2 hz

frequency

6. A student performs an experiment with a spring. In trial 1 the amplitude is 3cm, trial 2 it is 6cm. Compare the values of Period/Frequency/ and maximum speed between these two trials.

Period and Frequency remain the same

Doubling amplitude = 4x the energy 4x the energy is 2x the speed